

ORIGINAL ARTICLE

# Objective Morphological Classification of Neocortical Pyramidal Cells

Lida Kanari<sup>1</sup>, Srikanth Ramaswamy<sup>1</sup>, Ying Shi<sup>1</sup>, Sebastien Morand<sup>2</sup>, Julie Meystre<sup>3</sup>, Rodrigo Perin<sup>3</sup>, Marwan Abdellah<sup>1</sup>, Yun Wang<sup>4,5</sup>, Kathryn Hess<sup>2</sup> and Henry Markram<sup>1,3</sup>

<sup>1</sup>Blue Brain Project, Brain and Mind Institute, EPFL, Campus Biotech: CH 1202, Geneva, Switzerland,

<sup>2</sup>Laboratory for Topology and Neuroscience, Brain Mind Institute, EPFL, CH 1015, Lausanne, Switzerland,

<sup>3</sup>Laboratory of Neural Microcircuitry, Brain Mind Institute, EPFL, CH 1015, Lausanne, Switzerland, <sup>4</sup>School of Optometry and Ophthalmology, Wenzhou Medical College, Wenzhou, Zhejiang 325035, PR China and <sup>5</sup>Allen Institute for Brain Science, Seattle, WA 98109, USA

Address correspondence to email: lida.kanari@epfl.ch; henry.markram@epfl.ch

Lida Kanari, Srikanth Ramaswamy and Ying Shi are Co-first authors

Yun Wang, Kathryn Hess and Henry Markram are Senior authors

## Abstract

A consensus on the number of morphologically different types of pyramidal cells (PCs) in the neocortex has not yet been reached, despite over a century of anatomical studies, due to the lack of agreement on the subjective classifications of neuron types, which is based on expert analyses of neuronal morphologies. Even for neurons that are visually distinguishable, there is no common ground to consistently define morphological types. The objective classification of PCs can be achieved with methods from algebraic topology, and the dendritic arborization is sufficient for the reliable identification of distinct types of cortical PCs. Therefore, we objectively identify 17 types of PCs in the rat somatosensory cortex. In addition, we provide a solution to the challenging problem of whether 2 similar neurons belong to different types or to a continuum of the same type. Our topological classification does not require expert input, is stable, and helps settle the long-standing debate on whether cell-types are discrete or continuous morphological variations of each other.

**Key words:** neuronal classification, neuronal morphology, pyramidal cells, rat somatosensory cortex, topological data analysis

## Introduction

The mammalian neocortex is comprised of about 85% excitatory pyramidal cells (PCs), and around 15% inhibitory interneurons (Cajal Santiago Ramon y 1911; DeFelipe and Fariñas 1992; Spruston 2008; Markram et al. 2015; Ramaswamy and Markram 2015). PCs, also termed principal cells, are characterized by a

triangular soma, 2 distinct dendritic domains, both of which exhibit a high density of spines, emanating from the base (basal dendrites) and the apex of the soma (apical dendrites, respectively), and an axon that usually forms several local collaterals before leaving the neocortex to project to distant brain regions. Basal dendrites are localized around the soma while apical

dendrites typically extend towards the Pia, forming multiple oblique dendrites en route and terminating in a distinct tuft that is associated with high branching density.

Apical dendrites impart unique functional properties to PCs and form the basis for the generation of active dendritic (Cuntz et al. 2007, van Elburg and van Ooyen 2010, Cuntz 2012, Ooyen and Elburg 2013, Bird and Cuntz 2016) and synaptic events, such as back-propagating action potentials (Stuart and Sakmann 1994), calcium transients in dendrites (Markram and Sakmann 1994; Schiller et al. 1995), integration of synaptic inputs from different cortical layers (Larkum et al. 1999, 2001; Schaefer et al. 2003; Spruston 2008), and spike-timing dependent plasticity (Markram 1997; Sjöström et al. 2001; Froemke et al. 2005). The unique functional properties of apical dendrites are therefore essential for integrating top-down (from association areas) and bottom-up streams of input (from primary sensory and motor areas) to the neocortex to shape the output firing pattern of PCs.

The characteristic morphological shapes of apical dendrites are associated with their unique functional properties, as objectively defined types of PCs also express unique firing patterns (Deitcher et al. 2017) and form distinct synaptic subnetworks within and across layers (Yoshimura et al. 2005; Kampa et al. 2006). Therefore, the branching properties of the apical trees are commonly used for their separation into morphological cell types (Ascoli and Krichmar 2000, Oberlaender et al. 2011, Marx and Feldmeyer 2012, Narayanan et al. 2017). The “expert classification,” which is based on visual inspection of the cells, usually makes it possible to distinguish the different shapes of morphologies and to group neurons into cell types. However, despite the expertise involved, visual inspection is subjective and often results in nonconsensual and ambiguous classifications (Ledergerber and Larkum 2010, Marx and Feldmeyer 2012, DeFelipe et al. 2013, Markram et al. 2015). A striking indication of this problem, as described previously (DeFelipe et al. 2013), is the fact that experts assign a different cell type to a neuron from the one they had chosen in their original study for the same neuron, independently of the reconstruction quality (DeFelipe et al. 2013).

For this reason, an “objective morphological classification” is essential for a consensual and consistent definition of neuronal types that can be achieved by either a “supervised” or an “unsupervised classification” scheme. The “objective supervised classification” starts from the expert classification and verifies or disproves a proposed grouping based on objective measurements. When the expert classification cannot be supported by objective measurements, an “objective unsupervised classification” scheme is required. In this case, the classifier starts from a random classification and reassigns labels to the cells based on objective measurements until the classifier converges to a stable grouping proposal.

To perform objective classification, the neuronal morphologies must be encoded in a digital format. The 3D digital reconstruction of a neuron encodes the path (in XYZ coordinates) and the thickness of each branch within its morphology and enables the consistent morphological analysis of its structure. The standard morphometrics (such as section length, bifurcation angles, etc.) (Ascoli and Krichmar 2000, Petilla Interneuron Nomenclature Group et al. 2008) that are commonly used as input measurements for objective classification, focus on different local aspects of the neuronal morphology and therefore must be used in combination with other morphological measurements. To avoid overfitting, that is, confusing the random noise in the biological structure with a significant discrimination factor, which is a result of using a large number of features in a few individual cells, feature selection is required. Appropriate

feature selection is important for identifying the features that are indicative of the differences between neuronal shapes and that can be generalized across different brain regions and species. However, feature selection is often subjective, and the feature sets proposed by different experts are often inconsistent (DeFelipe et al. 2013). In addition, alternative sets of morphometrics result in different classifications. To avoid this issue, a number of mathematically rigorous methods have been proposed for the morphological analysis of neurons (Van Pelt et al. 1992, DeFelipe et al. 2013, Gillette and Ascoli 2015, Gillette et al. 2015, Wan et al. 2015). We have developed an alternative representation of morphologies based on persistent homology (Carlsson 2009) that provides a standardized quantification of neuronal branching structure.

The Topological Morphology Descriptor (TMD) algorithm generates a barcode from a neuronal tree, coupling the topology of the branching structure with its geometry, and therefore encoding the overall shape of the tree in a single descriptor (Kanari et al. 2010). The TMD is a simplified representation of the original tree that retains key information to perform well in a discrimination task, by mapping the tree to a topological representation with less information loss than the usual morphometrics. The objective of this method is to render the morphological classification consistent and independent of manual grouping. The cell types proposed based on the TMD-classification are unbiased, since they are based on a mathematical descriptor of the tree's branching structure rather than the visual inspection of the cells, and thus this method is less prone to user-induced biases. In particular, there is no need to manually combine selected morphometrics in order to objectively support a proposed grouping, thus, avoiding overfitting by implicitly accounting for the correlations between features that are incorporated into their TMD profile.

Using this topological representation, we were able to establish that the cortical PCs can be objectively classified, based on their morphology, using only the branching structure of their apical dendrites. We compared the results of the topological classification to the expert-proposed cell types (Wang et al. 2018) and illustrate that the majority of subjective cell types can be objectively supported, with the exception of L5 subtypes (TPC\_A and TPC\_B) and the rare horizontal PCs that are found in L6.

In this study, we focused on morphological classification with the aim to enable classification of neurons for which experimental data does not comprise genetic or other forms of data except morphology. This is the first step towards a consensus of PC classes that require the detailed characterization of individual neurons in multiple dimensions, that is, morphological, physiological, and molecular. It is however important to start by distinguishing cells based on a reduced number of primary morphological types in order to further investigate the relation of the cellular morphology to the molecular and functional aspects of neurons, which is not yet fully understood.

## Materials and Methods

### Staining and Reconstruction Techniques

All animal procedures were approved by the Veterinary Authorities and the Cantonal Commission for Animal Experimentation of the Canton of Vaud, according to the Swiss animal protection law.

The 3D reconstructions of biocytin-stained PC morphologies were obtained from whole-cell patch-clamp experiments on 300  $\mu\text{m}$  thick brain slices from juvenile rat somatosensory cortex, following experimental and postprocessing procedures as previously described (Markram et al. 1997, Hughes et al. 2000,

Pawelzik et al. 2002, Wang 2002, Wang et al. 2004, Be et al. 2006). The neurons that were chosen for 3D reconstruction were high contrast, completely stained, and had few cut arbors. The details of the reconstruction method are described in the Supplementary Information. Reconstruction resulted in a set of connected points traced from the image stacks of the 3D neuronal morphology, each having a 3D (X, Y, Z) position and diameter. The reconstructed PCs from all layers of rat somatosensory cortex were then used for the topological classification.

### Visualization of Morphologies

The reconstructed morphology skeletons are represented by connected sets of points that account for the neurites and 2D profiles of somata. Accurate visualization of these morphologies requires simulating the 3D profile of the soma. We used a recent method to build a surface mesh model of the entire skeleton that represents its surface membrane. This method simulates the soma growth using Hooke's law and mass-spring systems (Abdellah et al. 2017).

### Topological Classification

For the topological classification, we first separated the PCs into layers according to the location of their somata, as labeled by experts during the reconstruction process. Because the definition of layers is not fully unambiguous, only cells that were clearly within layer boundaries were used; cells at the borders of layers were excluded from this study. The PCs were then separated into cell types based on the TMD of the branching patterns of their neuronal trees. The branching pattern of each tree is decomposed into a persistence barcode (Carlsson 2009). Each bar (specified by a pair of real numbers) of the barcode corresponds to the end and start radial distance from the soma of a branch within the tree. The algorithm that transforms the neuronal trees into the persistence barcodes was previously described in Kanari et al. (2018).

All the neurite types (basal, apical dendrites and axons) were analyzed. However, basal dendrites of PCs within the same layer exhibited no significant difference (see Supplementary Information). This is in agreement with a previous study in rodents that reports common morphological features of basal dendrites across different cortical regions (Bielza et al. 2014). On the contrary, the organization of basal dendrites in cortical layers across regions and species—primary visual area and prefrontal cortex in macaques—is anatomically distinct, such as the total extent, spine density and size (Elston 2003). Therefore, it appears that the geometry of basal dendrites does not generalize across cortical layers, regions, and species (Ramaswamy and Markram 2015). Local axonal morphology was also not a useful metric for the classification, because neuronal reconstructions contained few axonal branches and long-range axons were severed due to slicing artefacts. However, the use of the TMD of apical dendrites was sufficient for the rigorous separation of PCs into distinct classes. In order to take into account the orientation of the trees, for example, the inverted PCs, the radial distance was weighted according to the orientation of the tree towards the Pia. Use of alternative features as a representation function did not result in significant changes in the classification (see also Kanari et al. 2018), therefore, it was not necessary to combine multiple morphometrics for the results presented in the current study.

The TMD of the neuronal tree is used for the generation of the “persistence image” (Adams et al. 2017) of the tree, which summarizes the density of components at different radial

distances from the soma and can be used as input to various machine learning algorithms. We first performed a supervised classification using the cell types assigned by experts. An “objective supervised classifier” is trained on the cell types proposed by experts. Each neuron is then labeled according to its TMD profile. The accuracy of the classification is the proportion of TMD-labels that agree with the initial label. The classification is then repeated for a set of randomized labels corresponding to the initial number of cell types. If the expert classification accuracy is significantly higher than that of the randomized classification, the proposed grouping is accepted. If not, the expert classification cannot be confirmed by the TMD. The cell types are then redefined according to the TMD profiles of the neurons of the same layer, with the objective of determining an optimal separation between the defined cell types.

### Reclassification

The objective of the TMD-based classification is to test whether the expert types present distinct branching patterns and to explain the differences between them. However, in some cases the TMD-classification on the expert-proposed cell types indicates the existence of a large number of misclassified cells. This mismatch is caused either by the fact that these types differ in features orthogonal to the branching of the neurons, which are not captured by the TMD, or by the fact that the expert classification, which is prone to human error, does not take into account the branching. In the second case, the grouping can be improved by a semisupervised classification. Starting from the initial cell types, the misclassified cells are re-evaluated and distributed in new groups until the new grouping is stable. The reclassification is valid if the automatically assigned groups are better separated than the expert groups. If an optimal grouping is available, an objective clustering scheme can be proposed to replace the manually assigned types.

A measurement for the assessment of misclassification is the “confusion matrix.” In the context of supervised classification, the confusion matrix, also known as “error matrix” (Stehman 1997) is used to illustrate the performance of an algorithm. The name “confusion matrix” stems from the fact that it makes it easy to see if the system is confusing 2 types (i.e., commonly mislabeling one as another). Each row of the matrix represents the predicted type while each column represents the expert type (or vice versa). The value of the matrix at row *I*, column *J* is the percentage of cells that are of type *J*, according to the experts, while the classifier predicts that they are of type *I*. If all predicted labels are the same as the expert labels, the diagonal of the matrix will be 1 (100% accuracy), and the rest of the matrix will be 0, indicating that the total error is 0%.

### Accuracy of Classification

The accuracy of the TMD classifier reported in this study is based on the distance between the persistence images of the apical dendrites of the neurons. However, when reclassification is required, the accuracy cannot be computed in terms of the same distance, to avoid overfitting. In this case, the accuracy of the TMD-based classification is evaluated by the computation of a number of different topological distances between a pair of persistence diagrams derived from the neuronal trees. These distances are not entirely independent from the distance defined between persistence images, but they capture properties of the diagrams that have not been taken into account in the TMD-classifier. Therefore, the evaluation of the TMD-classifier based

on a number of “independently” computed distances will be more impartial. To evaluate TMD-classification performance, we computed the bottleneck distance (Edelsbrunner and Harer 2008), the Wasserstein distance (Villani 2003, Edelsbrunner and Harer 2010), the sliced-Wasserstein distance (Carrière et al. 2017), and a number of distances on the vectorized persistence diagrams: the distance between landscapes (Bubenik and Dlotko 2017) and the distance between signatures (Carrière et al. 2015). These distances are described in detail in the supplementary information (SI). The reported accuracy is computed as the average accuracy of the classification based on these distances.

## Results

We have characterized 5 major types of PCs (as illustrated in Fig. 1), in agreement with expert observations. BPC (bitufted PCs, found in L6) are identified by 2 apical trees extending to opposite directions: one towards the Pia and one towards the white matter. IPC (inverted PCs, found in L2 and L6) are identified by the main direction of their apical tree, which is oriented towards the white matter. HPC (horizontal PCs, found in L6) are also identified by the direction of their apical tree, which is oriented parallel to the pia, as opposed to all other types. The rest of the PC types are oriented towards the pia: TPC (tufted PCs, found across all layers), which are identified by a distinct tuft formation, distal from the soma; UPC (untufted PCs, found in deep layers 4, 5, 6), which lack a clear tuft formation but extend to large radial distances; and SSC (spiny stellate cells, found in L4), which also lack a tuft formation, but also extend to small radial distances. In addition, 3 subtypes of TPC cells have been identified (A, B, and C). TPC\_A cells are the largest tufted cells and form a distinct large tuft (highest density of branches) and multiple obliques. TPC\_B cells form a proximal tuft (close to the soma) that is larger than the tuft of TPC\_C cells but have few or no obliques. TPC\_C (previously termed slender-tufted PCs, Markram et al. 2015) form a small distal tuft and multiple obliques. The results of the topological analysis are described in the following section, organized by layers.

### PCs in Layer 2

The TMD clustering of L2 PCs ( $n = 43$ , Fig. 1) based on their apical trees illustrates the existence of 3 subtypes with accuracy 84% (this result is cross-validated with 5 additional topological

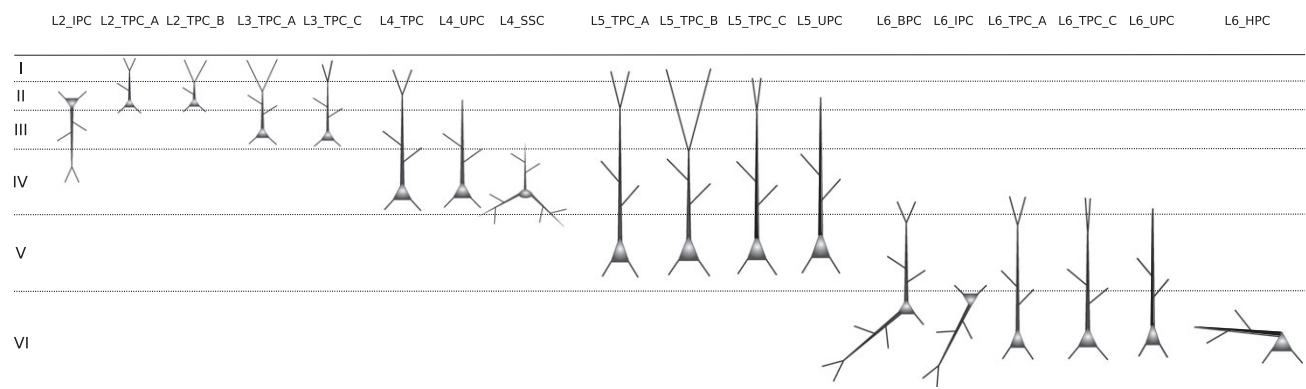
distances which yield an average accuracy of 83%). The L2\_IPCs (inverted PCs,  $n = 4$ ), which are directed towards white matter, have apical trees that project in the direction opposite to the pia, therefore generating a higher density of branches in this direction (Fig. 1). On the contrary, the L2\_TPCs (tufted PCs,  $n = 39$ ) contain apical dendrites that project towards the pia, therefore exhibiting a higher density of branches in this direction. Further analysis of the branching patterns of L2\_TPCs results in a separation into 2 subtypes (L2\_TPC\_A,  $n = 6$  and L2\_TPC\_B,  $n = 33$ ) depending on the density of branches on the distal apical dendrites: L2\_TPC\_A have a small density of branches within the tuft, while L2\_TPC\_B do not.

A quantitative analysis based on the morphometrics of 3D reconstructions of the 3 subtypes of PCs (L2\_IPC, L2\_TPC\_A, L2\_TPC\_B) revealed a small but not significant quantitative difference of average soma sizes; the average soma surface area of L2\_TPC\_B is larger (+10%) than the surface areas of L2\_TPC\_A and L2\_IPC somata. The basal dendrites of L2 PCs subtypes share similar morphological features, and therefore no morphological difference can be quantitatively justified. The average total length, surface area and volume of the apical dendrites of L2\_TPC\_B cells are larger than those of L2\_TPC\_A and L2\_IPC cells, reflecting their broader extents. In addition, L2\_TPC\_B axons extend further, resulting in larger total lengths and surface areas, suggesting the formation of dense local axonal clusters. However, the results about the axonal morphometrics are inconclusive due to the significant loss of axonal mass described in the previous sections.

Expert-based observations of the same dataset suggest the existence of 3 distinct types. L2\_IPC cells (inverted PC) have a vertically inverted apical dendrite projecting towards deep layers and white matter that forms a proximal or distal extensive tuft formation and multiple oblique dendrites. The apical dendrites of both L2\_TPC\_A and L2\_TPC\_B subtypes reach the pia and differ mainly in the bifurcating point along the apical dendrite where the tufts begin to form: proximal or distal. Therefore, the TMD-based classification supports the subjective observations for L2 PCs, and for consistency we use the expert-proposed terminology for those cell types.

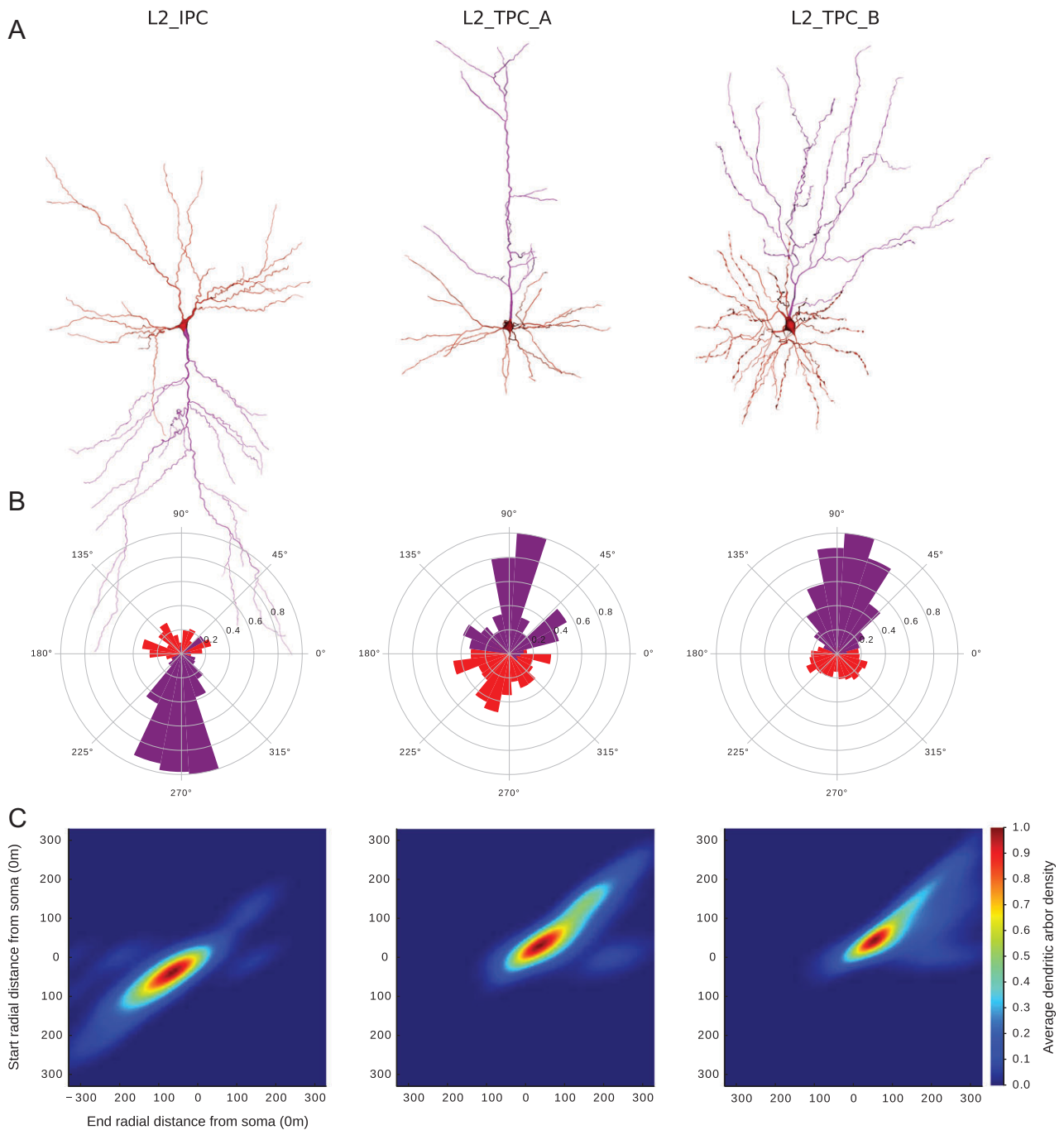
### PCs in Layer 3

The TMD clustering of L3 PCs ( $n = 44$ , Fig. 2) based on their apical trees illustrates the existence of 2 subtypes with accuracy



**Figure 1.** Schematic representation of all PC types/subtypes in Layers 2–6. Layer 2 consists of 2 main types of PCs, the L2\_IPC (inverted PCs) and the L2\_TPC (tufted PCs) which can be divided into 2 subtypes (A: large tufted PCs, and B: early bifurcating PCs). Layer 3 has one major type L3\_TPC and 2 subtypes of PCs (A – large tufted PCs, and C – small tufted PCs). Layer 4 PCs are grouped into 3 types (L4\_TPC; tufted PCs, L4\_UPC; untufted PCs and L4\_SSC; spiny stellate cells). Layer 5 PCs consist of 2 major types (L5\_TPC; tufted PCs and L5\_UPC; untufted PCs) and 2 subtypes of L5\_TPC (A – large tufted PCs, also known as thick tufted PCs and C – small tufted PCs, also known as slender tufted). Layer 6 consists of 5 major PC types: L6\_BPC (bitufted PCs), L6\_IPC (inverted PCs), L6\_TPC (tufted PCs), L6\_UPC (untufted PCs) and L6\_HPC (horizontal PCs). Also, 2 subtypes of L6\_TPC are identified (A: large tufted PCs, and C: small tufted PCs, also known as narrow tufted).





**Figure 2.** Three PC types/subtypes in Layer 2. (A) Exemplar reconstructed morphologies of PC dendrites: the apical dendrite is presented in purple and the basal dendrites in red. (B) Polar plot analysis of dendritic branches (apical in purple, basal in red). Tufted PCs are oriented towards the pia and the inverted PCs in the opposite direction as they project towards the white matter. (C) The Topological Morphology Descriptor (TMD) of apical dendrites characterizes the spatial distribution of branches with respect to the radial distance from the neuronal soma. The average persistence images (per type of PC) illustrate the average dendritic arbor density around the soma. The spatial distribution of L2\_IPC apical branches follow the direction opposite to the pia, while L2\_TPC\_A, which head towards the pia, present a larger density of branches for larger radial distances compared with L2\_TPC\_B.

89% (this result is cross-validated with 5 additional topological distances that yield an average accuracy of 85%). The L3\_TPC\_A ( $n = 34$ ) have apical trees with high density of branches close to the soma, but lower density of branches within the tuft. On the contrary, apical dendrites of L3\_TPC\_C ( $n = 10$ ) have a smaller density of branches around the soma, but higher density of branches on the tuft.

Quantitative morphological analysis on the 2 subtypes of L3 PCs (L3\_TPC\_A, L3\_TPC\_C) does not reveal any significant differences in the somatic and axonal features of the 2 subtypes. The differences between the 2 subtypes are captured only by the morphometrics of the apical dendrites. On average, L3\_TPC\_A cells have a larger number of oblique dendrites than L3\_TPC\_C cells, which corresponds to the lower densities of the latter

observed in their persistence images. In addition, L3\_TPC\_A apicals have larger average lengths, surface areas, and volumes than L3\_TPC\_C.

Expert-based observations of the same dataset suggest the existence of 2 distinct types of L3 PCs, both of which are oriented towards the pia: the L3\_TPC\_A have a vertically projecting apical dendrite, with an often distal (occasionally proximal) onset of tuft formation, which forms a small tuft (occasionally extensive) and multiple oblique dendrites before tuft formation. On the contrary, the L3\_TPC\_C have a vertically projecting apical dendrite with distal onset of tuft formation, which forms a small tuft and few oblique dendrites before formation of the distal tuft. Therefore, the TMD-based classification supports the subjective observations of 2 subtypes in L3 PCs.

Compared with PCs in superficial layers (L2; Fig. 1), L3 PCs appear to be larger on average, presenting larger extents and higher densities of branches, associated with larger total lengths. However, individual cells of L3 can be smaller than L2 cells, indicating that they cannot be distinguished merely by standard morphometrics. As a result, the information of soma location is essential for the analysis of L2 and L3 PCs. The axonal bouton density of L2 and L3 PCs is similar: with an average of 18–21 boutons/100  $\mu\text{m}$ . Previous studies examined L2 and L3 PCs together, yielding 2 subtypes, which primarily differ in axonal morphology (Larsen and Callaway 2005) and therefore cannot be objectively linked to the cell types defined in this study, which are separated based on their apical dendrites. A subtype of superficial L2/3 PC sends axonal collaterals into L3 and 5, lacking axonal arbors in L4 while the other subtype, which is usually located at the bottom border of L3 (close to L4), has significantly more axonal collaterals within L4.

The first case where reclassification is required is the L3 PC subtypes. Even though the score of the expert classification is high (86%), the confusion matrix (Fig. 3C,D) indicates that the 2 subclasses are frequently confused for one another. In addition, a visual inspection of the cells (Fig. 3A) illustrates that the 2 subclasses included cells with both large and smaller tufts and their structural differences are not easily identifiable.

The reclassification according to the TMD profiles of their apical trees proposed a separation into 2 subtypes: the first includes cells with small tufted apical dendrites and the second cells with large tufted apical dendrites. This grouping is stable with respect to the automatic classification (Fig. 3E,F), and visual inspection (Fig. 3B) of the reclassified cells confirms that the 2 suggested subtypes correspond to L3\_TPC\_A (large tufted PCs) and L3\_TPC\_C (small tufted PCs). The expert grouping included a subtype (L3\_TPC\_B) in which half of the cells were unambiguous (Fig. 3D). On the contrary the TMD-based clustering includes only one unambiguous cell (~2%, Fig. 3F) yielding a well-defined separation of L3\_TPC cells into the 2 proposed subtypes.

### PCs in Layer 4

The TMD clustering of L4 PCs ( $n = 89$ , Fig. 4) based on their apical trees illustrates the existence of 2 subtypes with accuracy 82% (this result is cross-validated with 5 additional topological distances that yield an average accuracy of 76%). The L4\_TPCs (tufted PCs,  $n = 44$ ) have a long apical tree that extends to large radial distances and forms a tuft that presents a high density of branches at radial distances that are distal from the soma. The L4\_UPCs (untufted PCs,  $n = 33$ ) apical trees also extend to large radial distances, but do not form a discrete tuft, as only few branches per tree reach the maximum radial distances. The apical trees of L4\_SSCs (spiny stellate cells,  $n = 12$ ) present a high density

of branches proximal to the soma, but only extend to small radial distances (about half of the radial distances of L4\_TPCs).

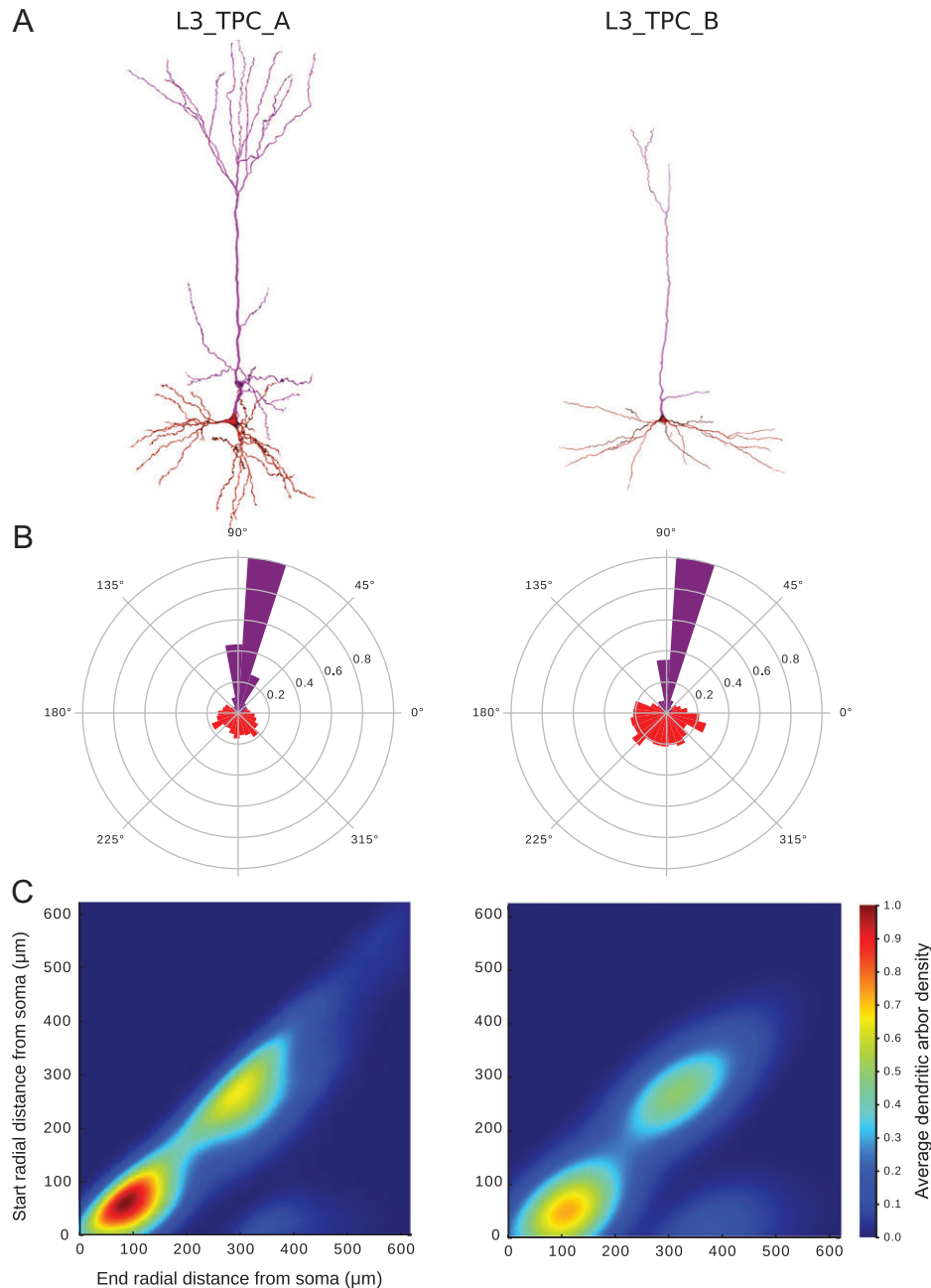
Quantitative analysis based on the morphometrics of 3D reconstructions of the 3 subtypes of L4 PCs (L4\_TPC, L4\_UPC, L4\_SSC) illustrates that L4\_SSC have smaller somata than L4\_TPC and L4\_UPC. On average, compared with L4\_UPC and L4\_SSC, L4\_TPCs have a larger number of basal dendrites, which are also significantly longer. Similarly, L4\_TPCs apical trees are bigger (larger total length, areas and volumes) than both other types, even though both L4\_TPC and L4\_UPC apical extents are significantly longer than those of L4\_SSC. Due to the significant loss of axonal mass, resulting from the slicing preparation (Stepanyants et al. 2009, Jaap et al. 2014), the results concerning the axonal morphometrics are inconclusive. However, the existence of 3 types is in agreement with previous studies that used thicker brain slices (500  $\mu\text{m}$  thick) (Staiger 2004) and reported 3 distinct types based on the axonal patterns of L4 PCs. In agreement with this study, the bouton density of L4\_UPCs ( $22 \pm 1$  boutons/100  $\mu\text{m}$ ) is higher than those of L4\_TPCs and L4\_SSCs ( $19 \pm 1$  and  $18 \pm 1$  boutons/100  $\mu\text{m}$  respectively).

Expert-based observations of the same dataset suggest the existence of 3 types of L4 PCs, based on their apical dendrites. The L4\_TPC (tufted PCs) have a vertically projecting apical dendrite with a small distal tuft and multiple oblique dendrites before tuft formation. The L4\_UPC (untufted PCs) have a vertically projecting apical dendrite without a tuft and multiple oblique dendrites that branch proximally to the soma. The L4\_SSC (spiny stellate cells) have a vertically projecting apical dendrite with small radial extents, not much longer than basal dendrites. Typically, the apical dendrites of all L4 PCs do not reach L1. Therefore, the TMD-based classification supports the subjective observations of 3 major types in L4 PCs.

### PCs in Layer 5

The TMD clustering of L5 PCs ( $n = 160$ , Fig. 5) based on their apical trees illustrates the existence of 2 subtypes with accuracy 90% (this result is cross-validated with 5 additional topological distances that yield an average accuracy of 84%). The TMD-based clustering of L5 PCs ( $n = 160$ , Fig. 5) based on their apical trees illustrates the existence of 3 subtypes of PCs that differ in the branching of their apical trees. The L5\_TPCs (tufted PCs) can be objectively separated into 2 subtypes: A and C. L5\_TPC\_A cells ( $n = 98$ ) have a long apical tree that extends to the largest radial distances, reaching L1. L5\_TPC\_A apical trees have 2 distinct clusters with a high density of branches, which differ in their radial distance from the soma. The cluster proximal to the soma corresponds to the rich oblique formation, while the region distal from the soma corresponds to the formation of a densely branching tuft. Similarly, the apical dendrites of L5\_TPC\_C ( $n = 32$ ) have 2 distinct clusters of high branching density, one proximal to the soma that corresponds to the obliques and one distal to the soma that corresponds to the tuft. However, the tufts of L5\_TPC\_C have a lower density of branches, even though they extend to large radial distances. L5\_UPC (untufted PCs,  $n = 30$ ) have a single high branching density cluster proximal to the soma, which corresponds to rich oblique formation. The reach of the apical trees of L5\_UPC is lower than the rest of L5 PCs, as the density of branches decreases with the radial distance from the soma, indicating the absence of a tuft.

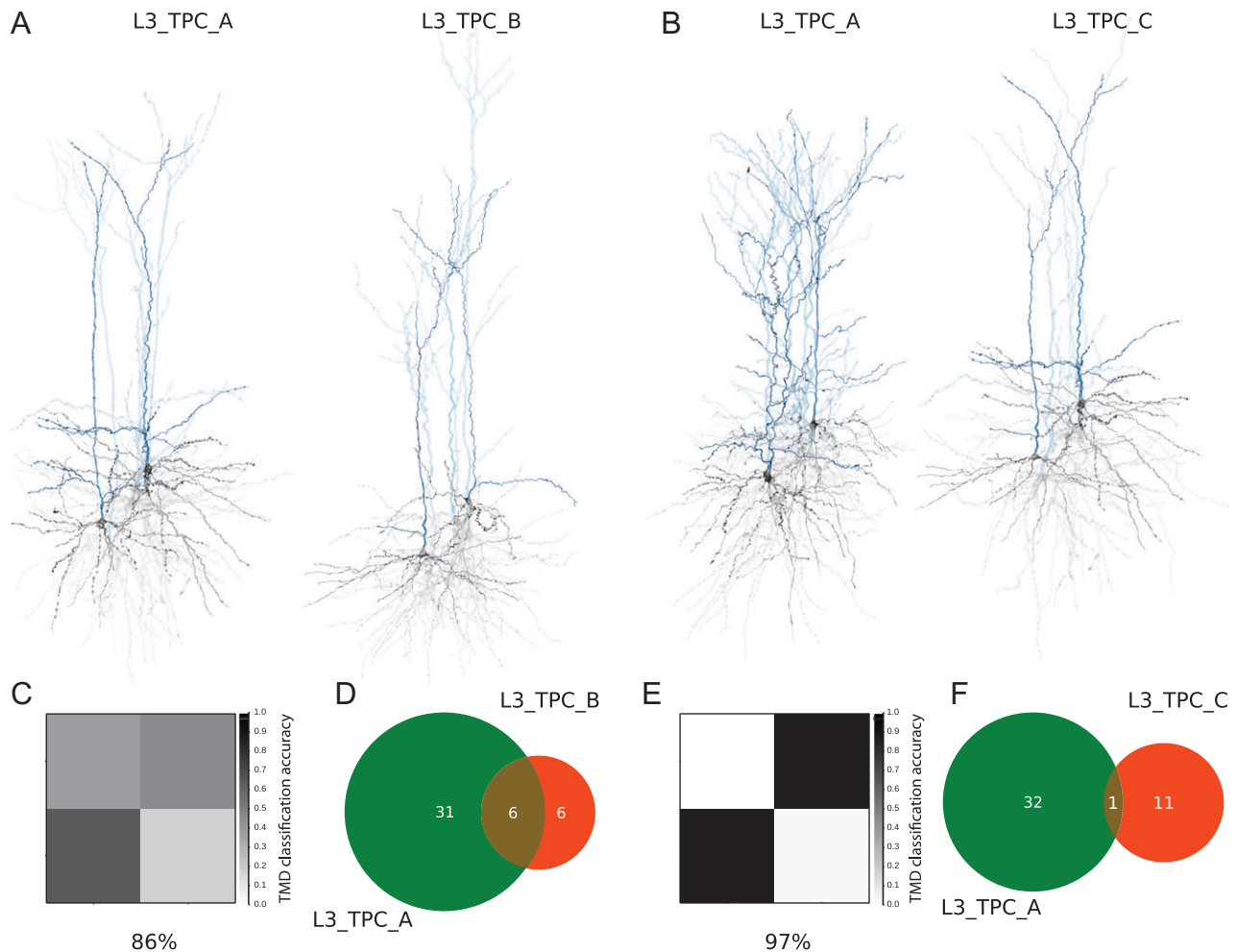
The quantitative analysis of 3D reconstructions of 3 subtypes of L5 PCs (L5\_TPC\_A, L5\_TPC\_C, L5\_UPC) showed that



**Figure 3.** Two PC types/subtypes in Layer 3. (A) Exemplar reconstructed morphologies. (B) Polar plot analysis of dendritic branches (apical in purple, basal in red). (C) The Topological Morphology Descriptor (TMD) of apical dendrites characterizes the spatial distribution of branches with respect to the radial distance from the neuronal soma. The average persistence images (per type of PC) illustrate the average dendritic arbor density around the soma. L3\_TPC\_C apical dendrites present a lower density of branches both close to the soma and at larger radial distances. L3\_TPC\_A are denser and extend to larger radial distances.

L5\_TPC\_A have significantly larger somata compared with L5\_TPC\_C and L5\_UPC. The basal dendrites of L5 PCs extend approximately to the width of a local cortical microcircuit (~300–500  $\mu\text{m}$ ), except those of L5\_UPCs, which are narrower. L5\_TPC\_A have a significantly larger basal dendritic surface area, which enables higher synaptic inputs than the 2 subtypes that have longer but thicker basal processes. The morphological properties of L5\_TPC\_A apical trees confirm the topological results. In addition, L5\_TPC\_A cells (15–16 boutons/100  $\mu\text{m}$ ) have bouton densities significantly lower than those of L5\_TPC\_C and L5\_UPCs (21 boutons/100  $\mu\text{m}$ ). Recent advances in retrograde

labeling of single neurons in vivo with recombinant rabies virus (Larsen 2008) resulted in the reconstruction of complete axons of L5 PCs, which supports the existence of 3 distinct subtypes based on their axonal properties. The thick-tufted PCs (corresponding to L5\_TPC\_A) project their local axons within deep layers, while the slender-tufted PCs (L5\_TPC\_C) and the short untufted PCs (L5\_UPCs) have extensive projections to supragranular layers. The axons of L5\_UPCs are relatively columnar, while those of L5\_TPC\_Cs have extensive lateral spreads within L2/3. Compared with in vivo labeling (Larsen 2008, Oberlaender et al. 2011), morphological measurements of axons obtained by



**Figure 4.** Reclassification of Layer 3 PCs. (A) Curated renderings of L3\_TPC\_A and L3\_TPC\_B selected morphologies as proposed by expert classification. (B) Curated renderings of L3\_TPC\_A and L3\_TPC\_B selected morphologies, after TMD-based reclassification. (C) The confusion matrix illustrates the large percentage of misclassified cells between the expert proposed subtypes, yielding a total accuracy of 86%. (D) The 2 subtypes are usually misclassified, as half of the L3\_TPC\_B are confused as L3\_TPC\_A. (E) The confusion matrix illustrates the clear separation of the 2 subtypes after the TMD-based reclassification and the improved accuracy of the classifier (97%). (F) The 2 subtypes are rarely misclassified, as almost all (~98%) of cells are unambiguously assigned into the 2 subtypes.

in vitro (300  $\mu$ m thick brain slices) labeling are underestimated, since the laterally spreading axonal processes are significantly severed during the slicing procedure.

Expert-based observations of the same dataset suggest the existence of 2 major cell types and 4 subtypes. The L5\_TPC\_A (thick-tufted PC\_A) have a vertically projecting apical dendrite with a distal broad, thick tuft and multiple oblique dendrites emerging proximally. The L5\_TPC\_B (thick-tufted PC\_B) are similar to the L5\_TPC\_A but further bifurcate into smaller tufts in comparison with L5\_TPC\_A. The L5\_TPC\_C (small-tufted PC) have a vertically projecting apical dendrite with a small distal tuft and multiple oblique dendrites emerging proximally. The L5\_UPC (untufted PC) have a vertically projecting apical dendrite with no tuft formation.

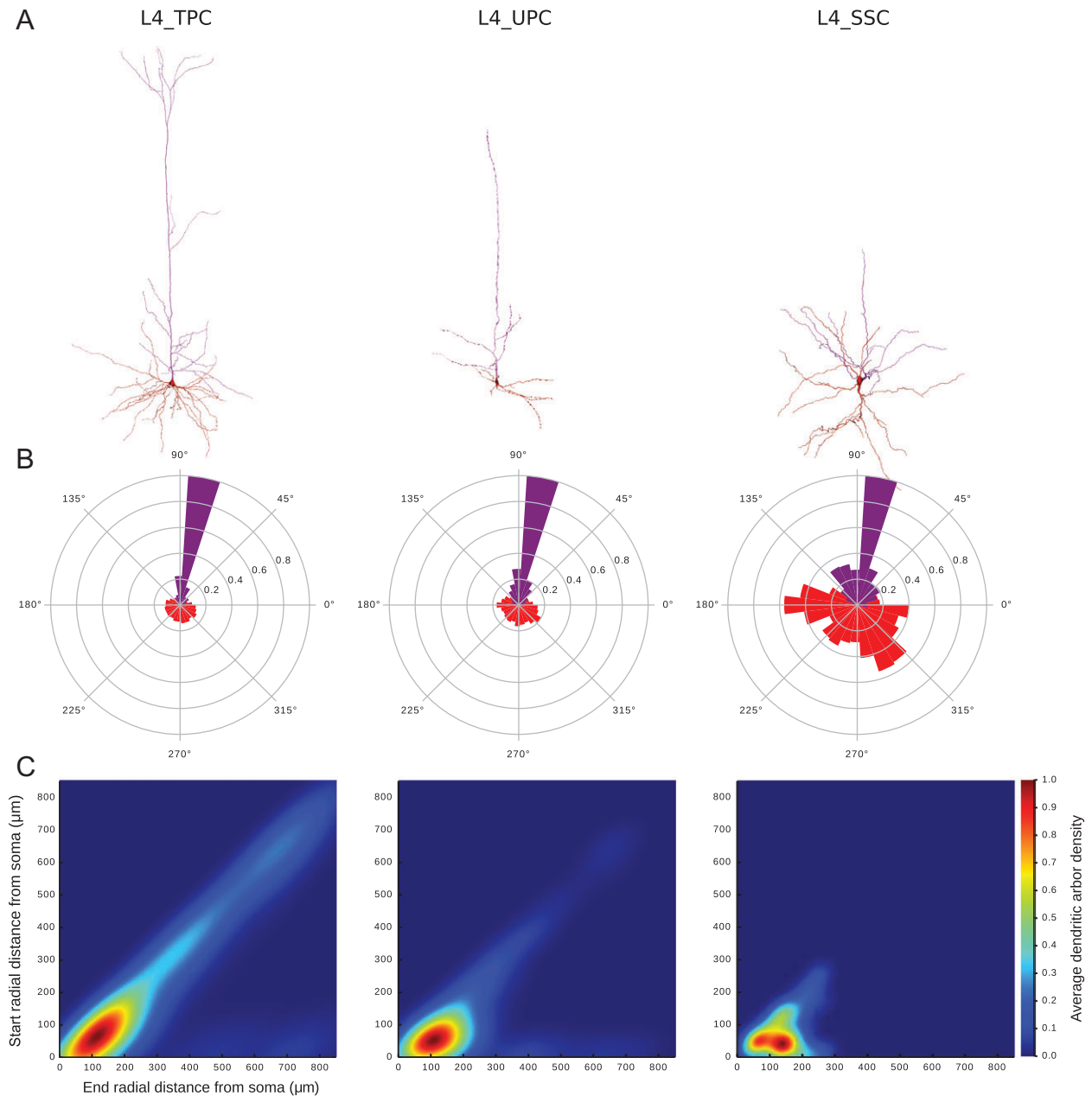
The expert classification into types L5\_TPC\_A and L5\_TPC\_B could not be validated by the TMD-based clustering, as no significant differences were found in the topological profiles of those subtypes. A reclassification based on the topological profiles of their apical trees, showed that there is a gradient between those 2 subtypes, as defined by experts, rather than a clear separation into 2 distinct types (Fig. 6). Carefully selected

exemplars of the 2 L5\_TPC subtypes show a clear divergence between them as their topological distance is significantly high (Fig. 6, right). However, the topological distance between cells of the 2 subtypes gradually decreases (Fig. 6, left) revealing a convergence between them. This analysis illustrates that the 2 subtypes belong to a continuum, rather than 2 distinctly separated types (Fig. 6). Therefore, the TMD-based classification supports the existence of 3 major types of L5 PCs, but not their separation into L5\_TPC\_A and L5\_TPC\_B subtypes. Further information, complementary to their branching structure, is required for the distinction of those subtypes, but was not available at the time of this study.

### PCs in Layer 6

The TMD clustering of L6 PCs ( $n = 123$ , Fig. 7) based on their apical trees illustrates the existence of 2 subtypes with accuracy 92% (this result is cross-validated with 5 additional topological distances that yield an average accuracy of 72%). L6\_BPC cells (bitufted PCs,  $n = 32$ ) are identified by 2 vertically projecting branching clusters that project to opposite directions. Both of the

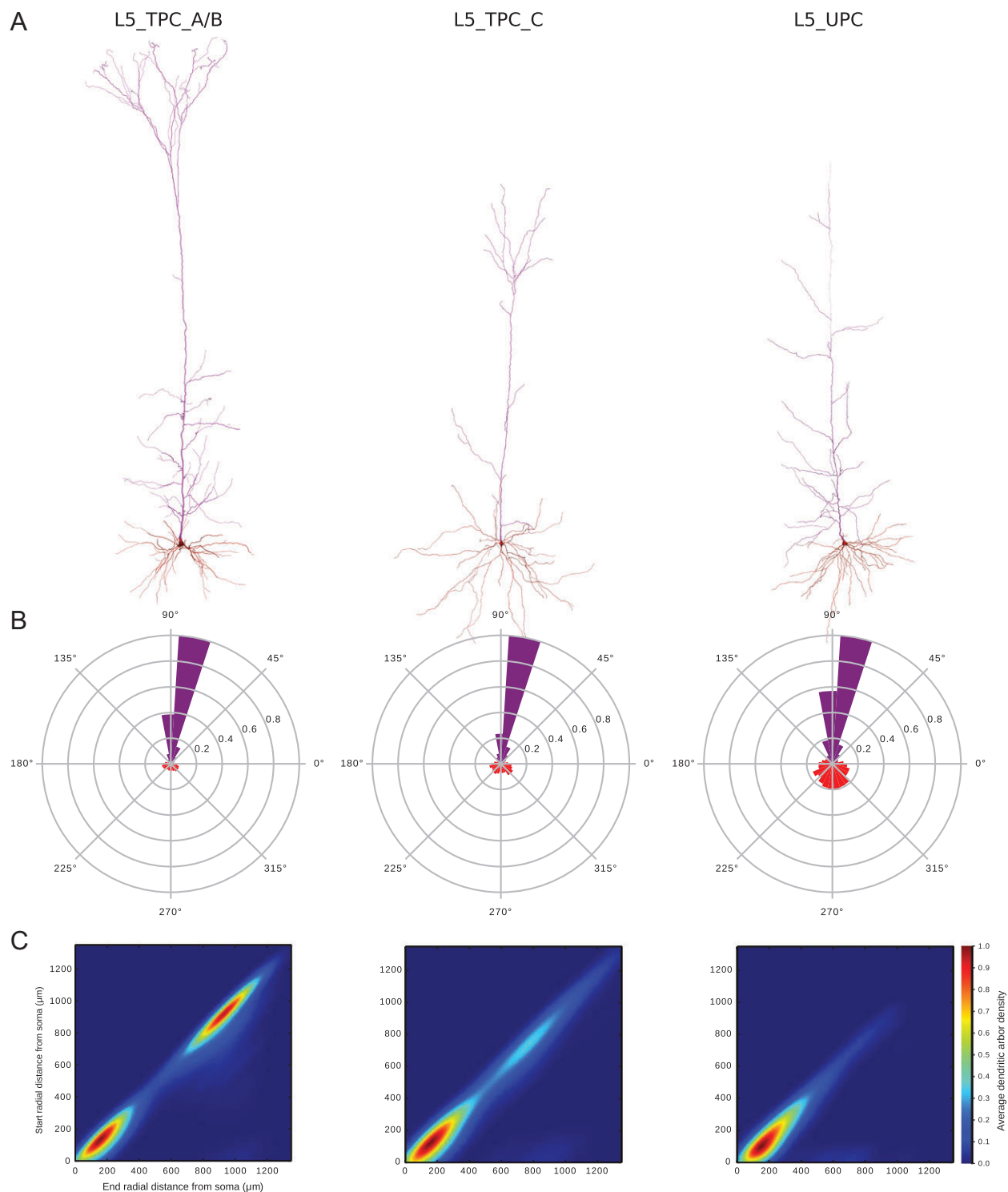




**Figure 5.** Three PC types/subtypes in Layer 4. (A) Exemplar reconstructed morphologies. (B) Polar plot analysis of dendritic branches (apical in purple, basal in red). The polar plots of all types are similar as they all project towards the pia, with the exception of L4\_SSC which remain local. (C) The Topological Morphology Descriptor (TMD) of apical dendrites characterizes the spatial distribution of branches with respect to the radial distance from the neuronal soma. The average persistence images (per type of PC) illustrate the average dendritic arbor density around the soma. The apical dendrites of L4\_TPC are the only ones that have a clearly defined tuft and are larger than both other types. L4\_SSC are smaller than L4\_UPC and their apical trees are similar to basal dendrites as they only extend to small radial distances.

apical trees of L6\_BPC form a small distal tuft, which is indicated by a small distal cluster of branches in the persistence image (Fig. 7), and a high density of branches close to the soma. L6\_IPC (inverted PCs,  $n = 26$ ) are identified by the orientation of their apical trees, which are directed towards white matter. The low distal branching density of the L6\_IPC apical indicates the existence of a small tuft. L6\_TPC (tufted PCs,  $n = 49$ ), which form a distinct, large tuft, can be separated into 2 subtypes, as in the case of L5 PCs. The L6\_TPC\_A cells ( $n = 22$ ) have a long apical tree that extends to large radial distances (and reaches L4) and forms 2 clusters of branches at different radial distances from the soma.

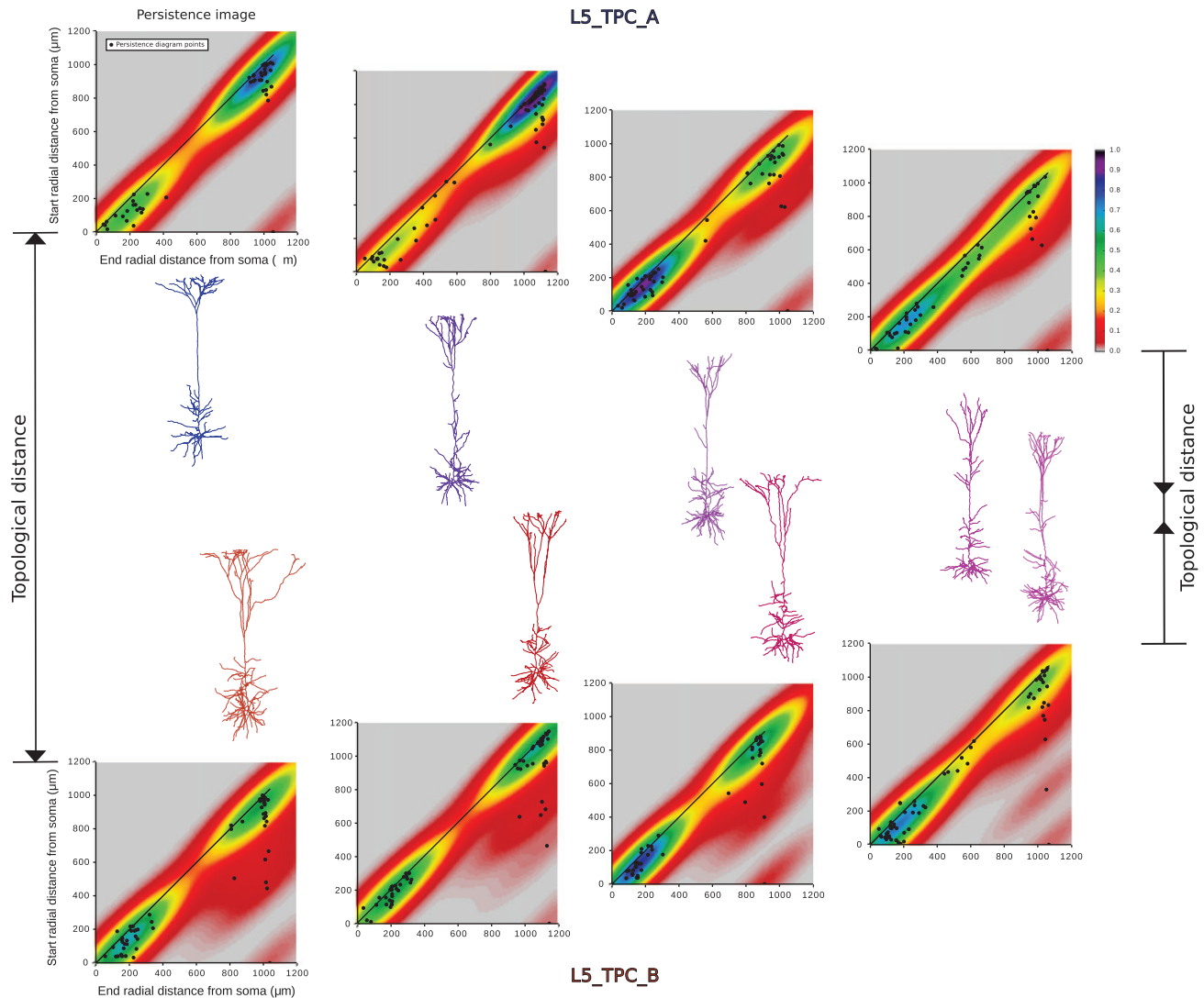
The cluster proximal to the soma corresponds to the rich oblique formation, while the distal cluster corresponds to the formation of a densely branching tuft. The L6\_TPC\_C cells ( $n = 27$ ) also have 2 distinct clusters of branches, one proximal to the soma that corresponds to the obliques and one distal to the soma that corresponds to the tuft. However, the tufts of L6\_TPC\_C have a lower density of branches than L6\_TPC\_A. L6\_UPC (untufted PCs,  $n = 16$ ) apicals have a single dense cluster of branches proximal to the soma, which corresponds to a rich oblique formation. L6\_UPC have smaller extents than L6\_TPC, and the density of branches decreases with the radial distance from the soma, indicating the



**Figure 6.** Three PC types/subtypes in Layer 5. (A) Exemplar reconstructed morphologies. (B) Polar plot analysis of dendritic branches (apical in purple, basal in red). The polar plots of all types are similar as they all project towards the pia. (C) The Topological Morphology Descriptor (TMD) of apical dendrites characterizes the spatial distribution of branches with respect to the radial distance from the neuronal soma. The average persistence images (per type of PC) illustrate the average dendritic arbor density around the soma. The apical dendrites of L5\_TPC\_A&B have a large tuft that extends to larger radial distances from the soma. L5\_TPC\_C similarly, present a tuft formation that is however smaller in size and extends to smaller radial distances. L5\_UPC do not present a clear tuft but can also reach larger radial distances.

absence of a tuft. Note that even though the 4 proposed types (and 2 subtypes of L6\_TPC) are consistent with the expert observations (see below), the individual cells were reclassified into

these groups according to their TMD profiles because the expert classification was based only on visual observations. The reclassification redistributed the misclassified cells and confirmed the



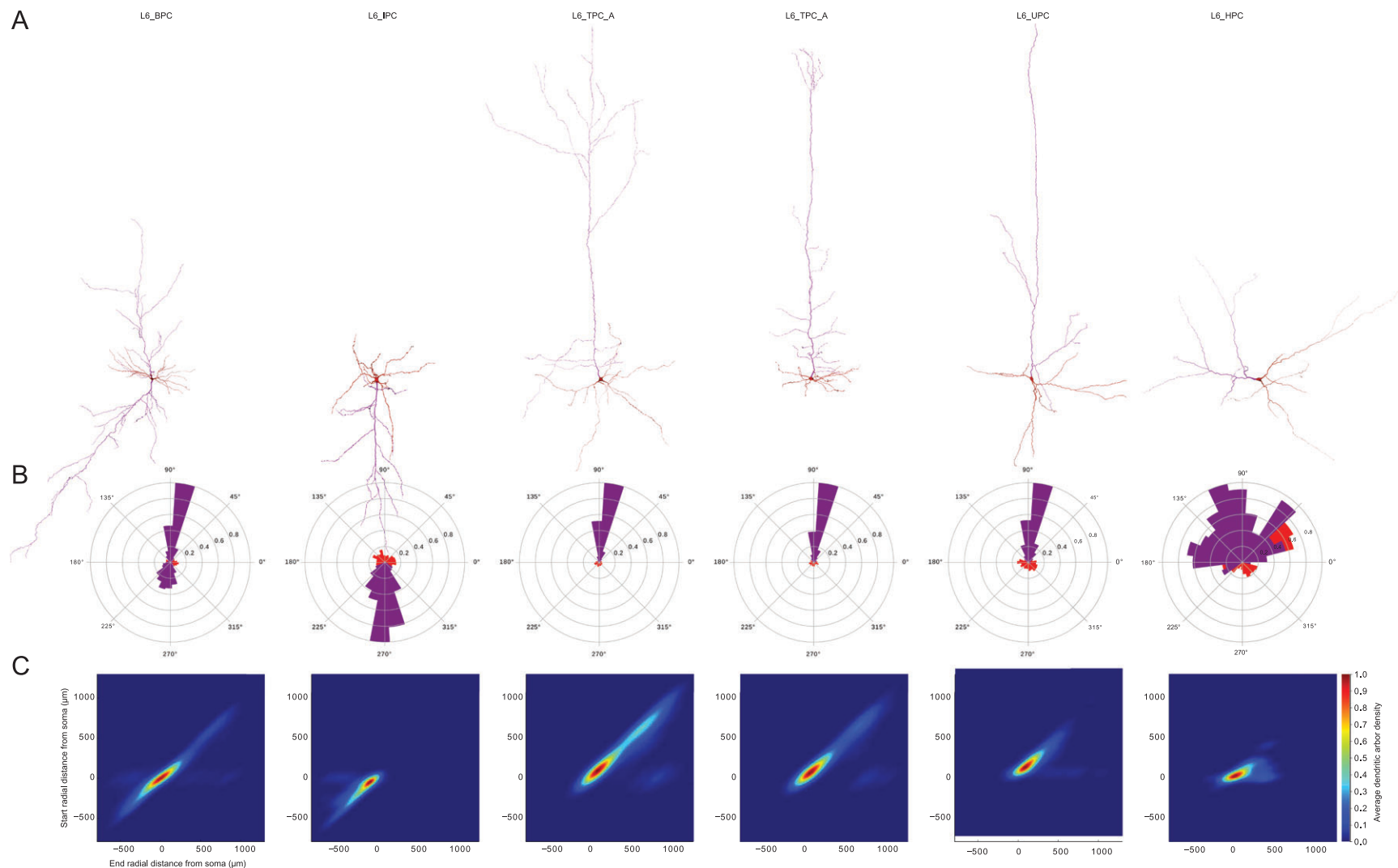
**Figure 7.** Convergence of subtypes L5\_TPC\_A and B. Illustration of selected dendritic morphologies of L5\_TPC\_A (in blue) and L5\_TPC\_B (in red) of decreasing topological distance (from left to right). For border cases the 2 subtypes are very well separated (extreme left). The persistence images of all the presented apical trees are shown, and the points of the persistence diagrams for each apical tree are superimposed on the respective persistence images. However, as the topological distance decreases as the persistence images converge (left to right), and morphologies exhibit similar topological shapes (extreme right).

existence of the expert-proposed groups with similar properties. The last subtype of L6 PCs is **L6\_HPC** (horizontal PCs). This subtype cannot be identified with the TMD-based classifier, as the apical dendrites of L6\_HPC have similar topological profiles to the L6\_UPCs. However, L6\_HPC have a preferred horizontal orientation, as opposed to all the other L6 PCs, and therefore they can be objectively distinguished if the main direction of the apical tree is taken into account.

The quantitative analysis based on the morphometrics of 3D reconstructions of L6 PCs (L6\_TPC\_A, L6\_TPC\_C, L6\_UPC, L6\_IPC, L6\_BPC, L6\_HPC) shows that the somata of L6\_HPCs are the biggest in L6 compared with other subtypes. L6\_TPC\_C basal dendrites are the smallest (minimum total length) among all L6 PCs, while the L6\_HPCs basal dendrites have the widest maximum horizontal extent, but the smallest number of dendritic trees. L6\_TPC\_As and L6\_UPCs have greater total dendritic length than all other L6 PCs, except HPCs. Quantitative analysis of L6 PCs axons demonstrates that they are largely similar, with the exception of L6\_TPC\_Cs, which have the narrowest

axonal trees with the smallest maximum horizontal extent, which is approximately equal to the width of a cortical column. In addition, the L6\_TPC\_Cs have the lowest bouton density (17 boutons/100  $\mu\text{m}$ ) and the L6\_HPCs the highest (22 boutons/100  $\mu\text{m}$ ). The other types/subtypes of L6 PCs all have similar bouton densities, ranging from 19 to 20 boutons/100  $\mu\text{m}$  on average. Since a significant part of the axons of L6 PC reconstructions cannot be retrieved due to the slicing of the tissue, as discussed in previous sections, especially since L6 axons typically extend through multiple cortical columns (Boudewijns et al. 2011), the morphometrics of L6 axonal branches will not be discussed further.

Subjective observations suggest the existence of 5 major types and 2 subtypes. The L6\_TPC\_A (tufted PC) have a vertically projecting apical dendrite with a small distal tuft and multiple oblique dendrites. The L6\_TPC\_C (narrow PC) have a narrow, vertically projecting apical dendrite, with a small distal tuft and often more oblique dendrites than other PC types. The L6\_UPC (untufted PC) have a vertically projecting apical



**Figure 8.** Six PC types/subtypes in Layer 6. (A) Exemplar reconstructed morphologies of (B). Polar plot analysis of dendritic branches (apical in purple, basal in red). The polar plots of L6\_BPC and L6\_IPC differ from other types that project towards the pia. Similarly, L6\_HPC is the only type which presents almost symmetric polar plots due to their horizontal orientation. (C) The Topological Morphology Descriptor (TMD) of apical dendrites characterizes the spatial distribution of branches with respect to the radial distance from the soma. The average persistence images (per type of PC) illustrate the average dendritic arbor density around the soma. L6\_BPC have 2 distinct apical trees, that extend to opposite directions. Apical dendrites of L6\_IPCs project away from the pia, towards the white matter. L6\_TPC\_As form a large tuft at large radial distances from the soma, while L6\_TPC\_Cs form a narrow tuft usually in smaller radial distances. Apical dendrites of L6\_UPCs do not form a clear tuft but extend to large radial distances. L6\_HPC is unique to layer 6 and projects vertically within the layer.



dendrite with no tuft formation, but multiple oblique dendrites. The L6\_IPC (inverted PC) have a vertically inverted apical dendrite projecting towards the white matter with a small distal tuft and multiple oblique dendrites. The L6\_BPC (bitufted PC) have 2 vertically projecting apical dendrites: one oriented toward the pia with a small distal tuft that forms multiple oblique dendrites and one inverted, projecting towards the white matter with a small distal tuft and multiple oblique dendrites. The L6\_HPC (horizontal tufted PC) have a horizontally projecting apical dendrite with a small distal tuft that forms a few oblique dendrites. The apical dendrites of L6 PCs often reach L4 or supragranular layers, but very rarely reach L1. Therefore, the TMD-based classification supports the existence of 5 subtypes in L6, and an additional cell type (L6\_HPC) can be identified by using the main orientation of the apical tree as a distinctive parameter.

The types of L6 PCs identified in this study are in agreement with the proposed types of L6 PCs in a previous study (Marx

and Feldmeyer 2012). L6\_BPC correspond to the “multipolar neurons” of the study by Marx and Feldmeyer (2012), L6\_IPC to “inverted neurons,” L6\_TPC correspond to the “pyramidal cells,” L6\_UPC to the “tangentially oriented neurons” and L6\_HPC to the “horizontally oriented neurons.” Using this analogy as an example, we can identify potential links between the locally defined types of PCs and their respective long-range projections, as proposed in literature.

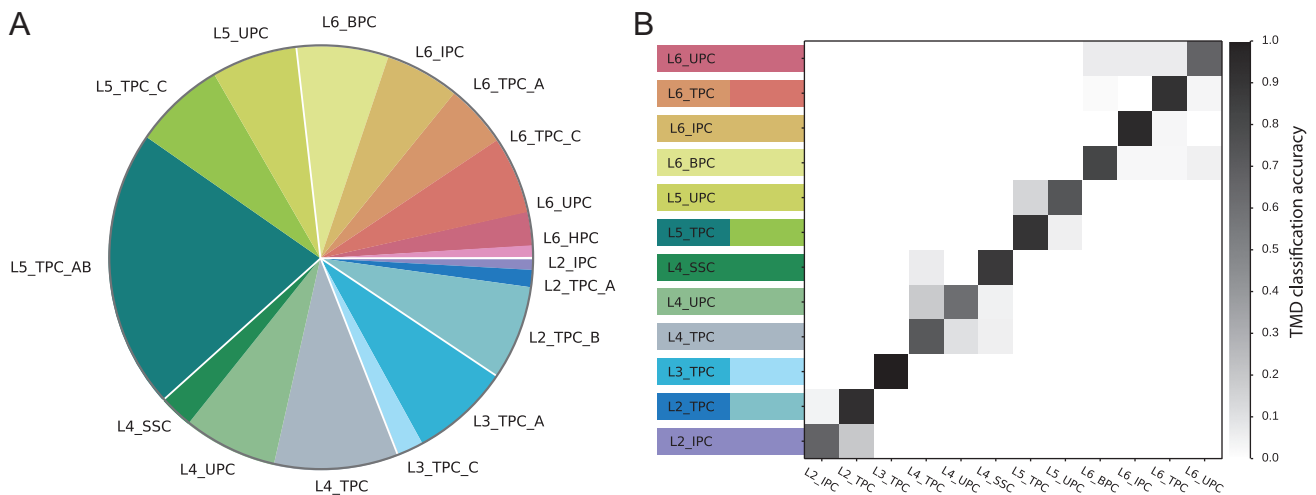
## Summary

The results of the TMD classification are summarized in Figure 8, where the percentage of occurrence of each m-type (Table 1, Fig. 8A) and the corresponding accuracy of the classification (Fig. 8B) are reported. The topological analysis of the branching structure of the PCs' apical dendrites revealed the existence of 16 subtypes of cells in all cortical layers, and one more subtype was objectively identified in L6 (Fig. 9). The objective classification justifies the existence of 3 subtypes in L2 (Fig. 1), 2 subtypes in L3 (Fig. 2), 3 subtypes in L4 (Fig. 4), 3 subtypes in L5 (Fig. 5), and 6 subtypes in L6 (Fig. 7). According to the laminar assignment of PCs by experts, no PCs were found in L1. The apical dendrites of PCs in supragranular L2/3 reach L1 and the pia. The apical dendrites of PCs in layers 4 and 6 often reach the supragranular layers, but not L1. Major PC subtypes in L5 have the longest apical dendrites, which reach L1 and the pia, and minor PC subtypes in L5 tend to extend to the supragranular layers, but not to L1 (Figs 10 and 9).

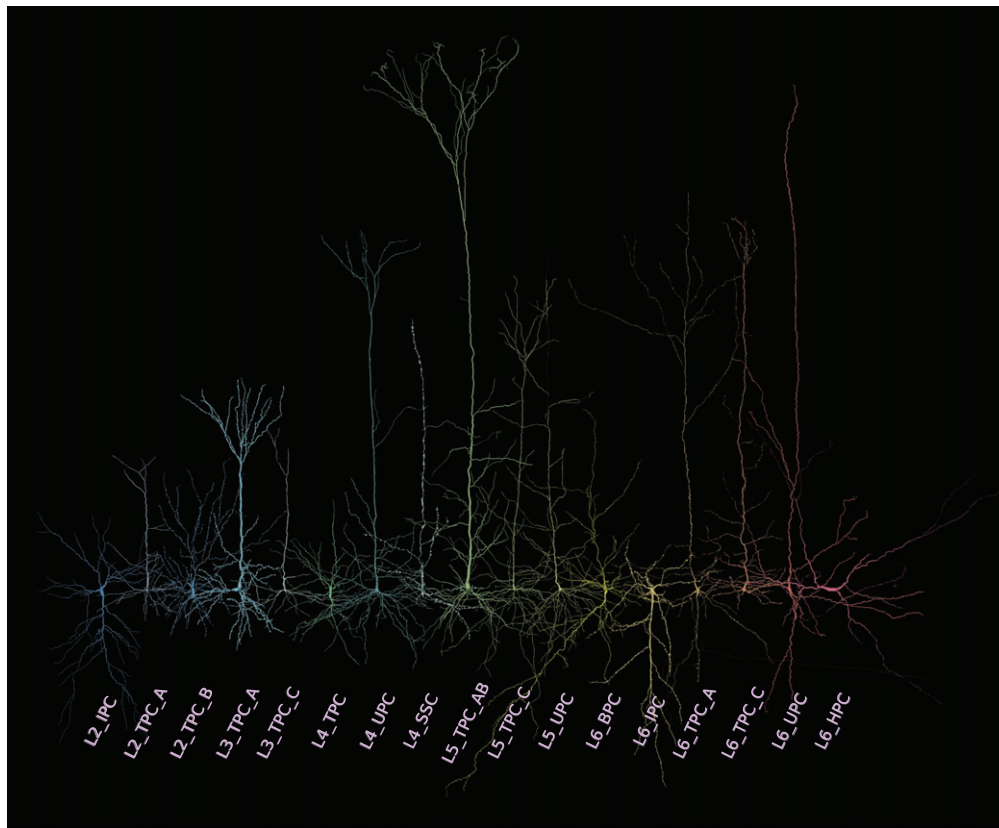
The expert analysis of the cells revealed the existence of 2 subtypes that are not justified by the topological analysis: a subtype of TPC cells in L5, and a horizontally oriented cell type in L6. The L5\_TPC subtypes proposed by the experts are related to the visual characteristics of the cells but cannot be confirmed by our objective characterization of the cells. Instead of a rigorous separation between these 2 subtypes, the TMD reveals that there is rather a continuous gradient between them. The second type not supported by the TMD, the L6\_HPC, can be distinguished by the main orientation of their apical dendrites, but the topological profiles of these cells are indistinguishable from the untufted L6 PCs (L6\_UPC). A reclassification was required for the definition of subtypes in Layers 3 and 5. In

**Table 1.** Number of PC types as identified by the TMD-based classification

Layer	Type of PCs	Subtype of PCs	Number of PCs	Percentage
2	IPC	–	4	0.86
2	TPC	A	6	1.29
2	TPC	B	33	7.10
3	TPC	A	33	7.10
3	TPC	C	11	2.37
4	SSC	–	12	2.58
4	TPC	–	44	9.46
4	UPC	–	33	7.10
5	TPC	A and B	98	21.07
5	TPC	C	32	6.88
5	UPC	–	30	6.45
6	BPC	–	32	6.88
6	HPC	–	7	1.50
6	IPC	–	26	5.59
6	TPC	A	25	5.38
6	TPC	C	22	4.73
6	UPC	–	17	3.66



**Figure 9.** Summary of TMD-based classification of all cortical PCs. (A) The pie-chart shows the percentage of cells per type/subtypes of cortical PCs, in different colors. The color-code is arbitrarily chosen. (B) The confusion matrix illustrates the accuracy of the classification for the TMD-defined classes. The values on the diagonal show the percentage of cells for which the automatic and input labels agree and illustrate the accuracy of the classification (black – high accuracy; white – low accuracy). The perfect classification would have only black on the diagonal and white everywhere else.



**Figure 10.** Overview of all cortical PCs types/subtypes. Renderings of dendrites and somata of all types/subtypes in order of appearance in the text. The color-code is arbitrarily chosen for consistency with Figure 8. Deeper layers express a larger diversity of PC types as the complexity of branching types increases from Layer 2 to Layer 6. The dendritic diameters have been scaled ( $\times 2$ ) for better resolution of the dendritic morphologies.

addition, L6\_TPC\_A, L6\_TPC\_C, and L6\_UPC were redefined according to the TMD classification.

## Discussion

Despite the expertise involved, visual inspection of neurons is subjective and often results in nonconsensual and ambiguous classifications (DeFelipe et al. 2013). In this study, we used a novel metric based on persistent homology (Kanari et al. 2018), which quantifies the branching structure of neuronal trees, to establish an objective standardized classification of PCs in the juvenile rat somatosensory cortex. We have demonstrated that the TMD of the apical dendrites of PCs is not only reliable in validating the quality of the expert classification but can also propose an alternative separation of cells into groups when the expert classification fails to provide a consistent definition of neuronal types.

Our classification scheme not only validates the existence of a common type of PCs across layers 2–6 (TPC) but also of several types that are unique to specific layers, such as the SSC in L4 and the BPC in L6. Interestingly, the diversity of shapes of apical dendrites increases with the distance from the pia, indicating that the higher functional complexity of deeper cortical layers can be successfully supported by the large morphological variability that is present in deeper layers, in agreement with recent observations (Reimann et al. 2017). The TMD-based classification was unable to distinguish a few cell types proposed by experts that differ in morphological characteristics that do not directly contribute to the branching structure, such as

L6\_HPC, which are distinguished by their horizontally oriented dendrites. In this particular case, an additional descriptor, that is, the main orientation of the cell, was used for the objective discrimination of L6\_HPC neurons. This demonstrates that expert classification is useful to guide further improvements of the method. However, the subjective classification schemes should be objectively validated to compensate for human bias. Therefore, objective classifiers trained to automatically assess new cell-types based on datasets procured from objectively validated m-types will be essential to overcome the inconsistencies of subjective morphological classification.

Certain tools of the new subfield of algebraic topology called topological data analysis (TDA) enable the study of multidimensional persistence (Carlsson and Zomorodian 2009, Sciamiero et al. 2016) of features and could be used for combining independent morphological measurements not currently considered in the computation of the TMD into multidimensional barcodes. Using this technique, independent characteristics could be combined into a single topological descriptor to strengthen even further its discriminative power. For example, cells that differ on parameters that are currently not considered, such as the thickness of the processes and the bouton density and cannot be distinguished with the TMD descriptor, could be discriminated by an extended multidimensional descriptor. This study is but the first step towards a generalized scheme of consistent cell types as it only takes morphological features into consideration. With the availability of new datasets combining physiological, genetic and morphological properties the multidimensional persistence could also enable the integration of independent parameters

towards an accurate classification of cell-types (Seki et al. 2010, Armañanzas and Ascoli 2015, Ecker et al. 2017, Li et al. 2017).

Another important characteristic that has not been included in this study and should ideally be combined in a refined version of the TMD descriptor, is the projection pattern of long-range axons that target distant brain regions. A growing body of evidence suggests a strong correlation between locally defined types of PCs and their target regions, which are genetically determined early on during differentiation and prior to the migration of the neurons to their destination layers (Mason and Larkman 1990; O'leary and Koester 1993, Kasper et al. 1994; Franceschetti et al. 1998; Gao and Zheng 2004; Larsen and Callaway 2005; Morishima 2006; Kumar and Ohana 2008; Marx and Feldmeyer 2012). Indeed, long-range axonal projection of PCs is an important feature that enables different computational functions and should therefore be taken into account for their classification (Larsen and Callaway 2005; Hattox and Nelson 2007; Larsen 2008; Brown and Hestrin 2009; Boudewijns et al. 2011).

Due to technical limitations, the long-range projections of PCs are not currently available for a sufficiently large number of cells to allow for their systematic characterization. However, recent advances in optical imaging and long-range axon labeling techniques are enabling a systematic reconstruction of single neurons at the whole-brain level (Yuan et al. 2015, Gong et al. 2016). Hopefully, these advances will lead to the systematic characterization of whole-cell reconstructions, in order to quantify their long-range axonal projection properties and associate them to their local dendritic properties.

## Supplementary Material

Supplementary material is available at *Cerebral Cortex* online.

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## Notes

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## Software availability

The software used for the extraction of the persistence barcodes from neuronal reconstructions will be available in the public domain <https://github.com/BlueBrain/TMD> under the GNU Lesser General Public License, version 3 (LGPLv3).

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